

Unit 1 – 7 Polynomials

Name: _____

Name	Examples	Non-Examples
Monomial (one term)	1. $3x^4$ 2. a^2 3. 5	degree:4 degree:2 degree:0
Binomial (two terms)	1. $2n^3 - n$ 2. $p - 3$ 3. $-3a^3b^4 + a^4b^5$	degree:3 degree:1 degree:9
Trinomial (three terms)	1. $-2x^3 + 2x - 3$ 2. $d(d^2 + 2d^4 - 2)$	degree:3 degree:5
Polynomial (one or more terms)	1. $3x^4 + 2x^3 - 5x + 1$ 2. $5y^6$ 3. $\frac{1}{2}x^2 + \sqrt{3}x^3 - 6x^4 + 1x - 3$	degree:4 degree:6 degree:4

1. EXPAND and SIMPLIFY (Also, list the degree and leading coefficient of your answer).

a. $(7x+3)-(2-2x)$

$$\begin{array}{r} 7x + 3 - 2 + 2x \\ \hline 9x + 1 \end{array}$$

$9x + 1$; DEG: 1 ; LC: 9

c. $3(x+5) + 8x$

$$\begin{array}{r} 3x + 15 + 8x \\ \hline 11x + 15 \end{array}$$

$11x + 15$; DEG: 1 ; LC: 11

f. $(2x^3 + 5x - 8) + (5x^3 - 9x^2 - 11x + 5)$

$$\begin{array}{r} 2x^3 + 5x - 8 + 5x^3 - 9x^2 - 11x + 5 \\ \hline 7x^3 - 9x^2 - 6x - 3 \end{array}$$

$7x^3 - 9x^2 - 6x - 3$; DEG: 3 ; LC: 7

b. $(5x^3 - 3x^4 - 2x - 9x^2 - 2) + (3x^3 + 2x^2 - 5x - 7)$

$$\begin{array}{r} 5x^3 - 3x^4 - 2x - 9x^2 - 2 + 3x^3 + 2x^2 - 5x - 7 \\ \hline -3x^4 + 8x^3 - 7x^2 - 7x - 9 \end{array}$$

$-3x^4 + 8x^3 - 7x^2 - 7x - 9$; DEG: 4 ; LC: -3

d. $-2(3x + 2y) - (5x - 6y) + 2x - 7$

$$\begin{array}{r} -6x - 4y - 5x + 6y + 2x - 7 \\ \hline -9x + 2y - 7 \end{array}$$

$-9x + 2y - 7$; DEG: 1 ; LC: -9, 2

e. $(2x^2 + 5x) - (6x^2 - 2x)$

$$\begin{array}{r} 2x^2 + 5x - 6x^2 + 2x \\ \hline -4x^2 + 7x \end{array}$$

$-4x^2 + 7x$; DEG: 2 ; LC: -4

g. $(2x+3)(3x-5)$

$$\begin{array}{l} \text{DISTRIBUTION} \\ (2x+3)(3x-5) \\ 3x(2x+3) - 5(2x+3) \\ 6x^2 + 9x - 10x - 15 \\ \hline 6x^2 - 1x - 15 \end{array}$$

$6x^2 - 1x - 15$; DEG: 2 ; LC: 6

h. $(2x-5)^2$

$$\begin{array}{r} (2x-5)(2x-5) \\ 4x^2 - 10x - 10x + 25 \\ \hline 4x^2 - 20x + 25 \end{array}$$

$4x^2 - 20x + 25$; DEG: 2 ; LC: 4

(1 Continued). EXPAND and SIMPLIFY

i. $4y^2(y^2 + 2y)$

$$4y^2 \cdot y^2 + 4y^2 \cdot 2y \\ 4 \cdot y \cdot y \cdot y \cdot y + 4y \cdot y \cdot 2 \cdot y$$

$$4y^2 + 8y^3; \text{ DEG:3 LC:8}$$

j. $-6y^2(3y^2 - 2y - 7)$

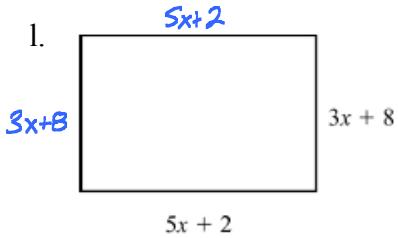
$$\underbrace{-6y^2 \cdot 3y^2}_{-18y^4} - \underbrace{(-6y^2)(2y)}_{12y^3} - \underbrace{(-6y^2)(7)}_{42y^2}$$

$$-18y^4 + 12y^3 + 42y^2; \text{ DEG:4 LC:-18}$$

k. $(x+3)(x+5)$

$$x^2 + \underbrace{5x + 3x}_{8x} + 15 \\ x^2 + 8x + 15$$

$$x^2 + 8x + 15; \text{ DEG:2 LC:1}$$



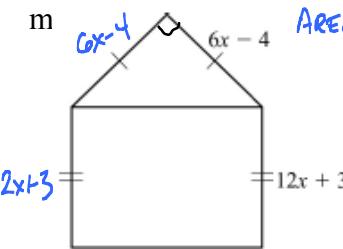
$$A = l \cdot w \\ A = (5x+2)(3x+8) \\ 15x^2 + \underbrace{40x + 6x + 16}_{16} \\ 15x^2 + 46x + 16$$

PERIMETER = $(5x+2) + (3x+8) + (5x+2) + (3x+8)$

Determine an expression that represents:

Perimeter = $16x + 20$ units

Area = $15x^2 + 46x + 16$ sq units



$$\text{PERIMETER} = (14x+13) + (12x+3) + (6x-4) + (6x-4) + (12x+3)$$

Determine an expression that represents:

Perimeter = $50x + 11$ units

Area = $186x^2 + 174x + 47$ sq units

$$\text{AREA } \Delta = \frac{b \cdot h}{2} = \frac{(6x-4)(6x-4)}{2} \\ = \frac{36x^2 - 24x - 24x + 16}{2} \\ = 18x^2 - 12x - 12x + 8 \\ = 18x^2 - 24x + 8$$

$$\text{AREA } \square = l \cdot w \\ = (14x+13)(12x+3) \\ = 168x^2 + 42x + 156x + 39 \\ = 168x^2 + 198x + 39$$

$$\frac{A}{\Delta} + \frac{\Delta}{\Delta} = \frac{168x^2 + 198x + 39}{186 + 174} + \frac{18x^2 - 24x + 8}{186 + 174}$$

2. Divide the following.

a. $\frac{32a^5 + 24a^3}{8a^3} = \frac{\cancel{32a^5}}{\cancel{8a^3}} + \frac{\cancel{24a^3}}{\cancel{8a^3}}$
~~4a²a²a~~ ↓ ↓
~~a²~~ $4a^2 + 3$

$$4a^2 + 3$$

b. $\frac{21x^4 + 3x^3}{3x^2} = \frac{\cancel{21x^4}}{\cancel{3x^2}} + \frac{\cancel{3x^3}}{\cancel{3x^2}}$
~~xx~~ ↓ ↓
~~xx~~ $7x^2 + 1x$

$$7x^2 + 1x$$

c. $\frac{36a^3d^5 + 72a^2d^3}{6ad^2}$
~~36aaaddd~~ ~~72aaddd~~
~~6aadd~~ ~~6aadd~~

$$6a^2d^3 + 12ad$$

3. Factor the GCF from each expression

a. $15x^4 + 3x^5$
~~3~~ ~~5xxx~~ + ~~3~~ ~~xxxxx~~

$$3x^4(5 + x)$$

$$a. 3x^4(5+x)$$

b. $16x^2 + 24$
~~4~~ ~~4~~ ~~6~~ ~~4~~
~~2.2.2~~ ~~2.x.x~~ + ~~3.2.2.2~~

$$8(2x^2 + 3)$$

c. $18x^4y^7 + 36x^3y^6 - 42x^5y^5$
~~3~~ ~~2~~ ~~xxx~~ + ~~3~~ ~~2~~ ~~xxx~~ - ~~3~~ ~~2~~ ~~xxxx~~

$$c. 6x^3y^5(3xy^2 + 6y - 7x^2)$$

d. $3x(x-3) + 2(x-3)$

$$(x-3)(3x+2)$$

$$b. 8(2x^2 + 3)$$

$$d. (x-3)(3x+2)$$

$$6x^3y^5(3xy^2 + 6y - 7x^2)$$